

DATA ANALYSIS (DAY 5) NOTES

VOCABULARY

Independent Events (an example of a compound event)

Definition:

two events occur if one event does not affect the occurrence of the other.

Formula:

$$P(A \text{ and } B) = P(A) \cdot P(B)$$

Dependent Events (an example of a compound event)

Definition:

two events occur if one event does affect the occurrence of the other.

Formula:

$$P(A \text{ and } B) = P(A) \cdot P(B, \text{ assuming } A \text{ occurred})$$

EXAMPLES

Decide whether the events are independent or dependent.

1. Each whole number from 1 through 10 is written on a piece of paper and placed in a hat. You randomly choose a piece of paper, do not put it back, then randomly choose another piece of paper.

EVENT A: Choose the 5 first.

EVENT B: Choose an odd number second.

Dependent events

2. You flip a coin and roll a number cube.

EVENT A: Get tails when flipping the coin.

EVENT B: Get a 2 when rolling the number cube.

Independent events

You roll a red number cube and a blue number cube. Find each probability. SIMPLIFY!

- 3.
- $P(\text{red } 2 \text{ and blue } 2)$

$$\frac{1}{6} \cdot \frac{1}{6} = \frac{1}{36}$$

- 4.
- $P(\text{red odd and blue even})$

$$\frac{3}{6} \cdot \frac{3}{6} = \frac{9}{36} = \frac{1}{4}$$

- 5.
- $P(\text{red greater than 2 and red } 4)$

$$\frac{4}{6} \cdot \frac{1}{6} = \frac{4}{36} = \frac{1}{9}$$

- 6.
- $P(\text{red odd and blue less than 4})$

$$\frac{3}{6} \cdot \frac{3}{6} = \frac{9}{36} = \frac{1}{4}$$

- 7.
- $P(\text{red } 6 \text{ and blue even})$

$$\frac{1}{6} \cdot \frac{3}{6} = \frac{3}{36} = \frac{1}{12}$$

- 8.
- $P(\text{red greater than 4 and blue greater than 3})$

$$\frac{2}{6} \cdot \frac{3}{6} = \frac{6}{36} = \frac{1}{6}$$

10 total marbles

You choose a marble at random from a bag containing 3 blue marbles, 5 red marbles, and 2 green marbles. You replace the marble and then choose again. Find each probability.

<p>9. $P(\text{both blue})$</p> $\frac{3}{10} \cdot \frac{3}{10} = \frac{9}{100}$	<p>10. $P(\text{both red})$</p> $\frac{5}{10} \cdot \frac{5}{10} = \frac{25}{100} = \frac{1}{4}$	<p>11. $P(\text{blue then green})$</p> $\frac{3}{10} \cdot \frac{2}{10} = \frac{6}{100} = \frac{3}{50}$
<p>12. $P(\text{red then blue})$</p> $\frac{5}{10} \cdot \frac{3}{10} = \frac{15}{100} = \frac{3}{20}$	<p>13. $P(\text{green then red})$</p> $\frac{2}{10} \cdot \frac{5}{10} = \frac{10}{100} = \frac{1}{10}$	<p>14. $P(\text{both green})$</p> $\frac{2}{10} \cdot \frac{2}{10} = \frac{4}{100} = \frac{1}{25}$

You choose a tile at random from a bag containing 2 tiles with X, 6 tiles with Y, and 4 tiles with Z. You pick a second tile without replacing the first. Find each probability.

<p>15. $P(X \text{ then } Y)$</p> $\frac{2}{12} \cdot \frac{6}{11} = \frac{12}{132} = \frac{1}{11}$	<p>16. $P(\text{both } Y)$</p> $\frac{6}{12} \cdot \frac{5}{11} = \frac{30}{132} = \frac{5}{22}$	<p>17. $P(Y \text{ then } X)$</p> $\frac{6}{12} \cdot \frac{2}{11} = \frac{12}{132} = \frac{1}{11}$
<p>18. $P(Z \text{ then } X)$</p> $\frac{4}{12} \cdot \frac{2}{11} = \frac{8}{132} = \frac{2}{33}$	<p>19. $P(\text{both } Z)$</p> $\frac{4}{12} \cdot \frac{3}{11} = \frac{12}{132} = \frac{1}{11}$	<p>20. $P(Y \text{ then } Z)$</p> $\frac{6}{12} \cdot \frac{4}{11} = \frac{24}{132} = \frac{2}{11}$

21. There are 12 girls and 14 boys in math class. The teacher puts the names of the students in a hat and randomly picks one name. Then the teacher picks another name without replacing the first. What is the probability that both students picked are boys?

26 total students

$$P(\text{both boys}) = \frac{14}{26} \cdot \frac{13}{25} = \frac{182}{650} = \frac{7}{25} \rightarrow 0.28 \rightarrow 28\%$$

12 total tiles